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Observer Design and Implementation for Packed-Bed Thermal Energy Storage Systems

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Abstract—This paper investigates the problem of designing a state observer for a Packed Bed Thermal Energy Storage System. In previous studies (see e.g. [21]), a mathematical model of the system, taking the form of two coupled partial differential equations, was derived and validated through comparison with experimental measurements. In this paper, the previously derived model is approximated by a lumped linear time-invariant model and then employed to design a Luenberger state observer capable of reconstructing the solid and fluid temperature profiles on the basis of few collocated fluid temperature measurements. Theoretical design and experimental results are presented throughout the paper.

Keywords. Thermal Energy Storage System. Sensible heat storage, Packed-bed technology; State observer.

I. INTRODUCTION

Model-based control and advanced process monitoring of Distributed-Parameter Systems (DPSs), governed by Partial Differential Equations (PDEs), tipically require full-state information. However, the available measurements of DPS'are typically located on collocated points of the spatial domain, that motivates the need of the state observer [17-20,23]. There are two main approaches to observer design in DPSs. In the first approach, the system PDEs are preliminarily discretized (by finite differences or finite volume method) and the observer design is subsequently made with reference to the obtained finite-dimensional approximate model. In the second approach, the observer is designed as an infinite-dimensional DPS, and discretization (tipically by finite differences) is made after, at the implementation stage. In this paper we take the former approach, by transforming the mathematical model of the system under consideration into an approximate Linear Time Invariant (LTI) finite-dimensional dynamics, and then applying observer design techniques for finite-dimensional LTI systems. The basic state estimator for linear, lumped-parameter systems is the Luenberger observer [22], which will be the observer considered in the present work within the framework of a physically-motivated observer design problem for a certain energy-storage engineering apparatus.

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Energy storage allows to efficiently exploit the renewable energy sources, which are inherently intermittent [1,2]. For concentrated solar power (CSP) plants in particular, storage of heat permits the uninterrupted production with and without the presence of the solar radiation [3-7]. In [5] the main thermal energy storage (TES) technologies were surveyed, and particularly the sensible heat storage and latent heat storage solutions were compared. Sensible heat storage raises the temperature of a solid medium, whereas the latent heat storage solution includes a phase change and implies the selection of an appropriate phase change material (PCM). Sensible heat storage is currently recognized as the simplest and cheapest method to store thermal energy [8]. Sensible heat TES systems with a single tank filled with solid material (packed bed) of high thermal capacity have been proposed, which are about 35% cheaper than the system with two tanks where the storage medium is the same heat transfer fluid (HTF) [9]. In the system with a single tank, the hot and cold fluids are separated by a moving region, called thermocline, which is characterized by a steep gradient of temperature that mainly depends on the characteristics of the solid storage material. Systems with packed bed (refractory ceramic materials, concrete, and limestone are most often utilized due to their relatively low cost and high thermal capacity) have been widely studied. Many published works (see e.g. [8, 10-14].) refer for numerical investigations to the mathematical PDE model originally developed by Schumann [12].

The main objective of the present work is to design and experimentally verify the performance of a state observer for a single tank packet-bed heat storage system. In a previous work [21] a mathematical model for the system in question was derived, taking the form of two coupled PDEs. In the present work, under sensible approximations, an approximate lumpedparameter LTI formulation of the model is derived. Such finite dimensional model is exploited to design a Luenberger observer. The performance of the observer are tested via comparison with temperature profiles acquired during experimental tests on a laboratory scale prototype operating at constant flow.

Section II recalls the considered mathematical model, with the Subsection II.A reporting the derivation of the approximate lumped-parameter LTI model. Section III presents the proposed Luenberger observer design and discusses the experimental investigation of the performance of the designed observer. Section IV draws some final conclusions and perspectives for next research.



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II. MATHEMATICAL MODEL OF THE THERMAL STORAGE SYSTEM

The Storage System consists of a thermally isolated cylinder filled with the packed bed solid material with high thermal capacity. During the loading phase, the hot HTF flows through the cylinder and conveys the thermal energy to the packed bed, whereas the reversed flow of the cold HTF is applied to collect the energy from the solid material in the discharging phase. The schematics and picture of the laboratory setup are shown in the Figures I.

The considered mathematical model is a LTNE (Local Thermal Non-Equilibrium) model based on Schumann's equations for heat transfer in a porous prism [12]. It consists of two coupled 1D PDEs which enable the calculation of the transient spatio-temporal evolution of the solid ($T_b(x,t)$) and fluid ($T_f(x,t)$) temperature under the assumptions that:

- The temperature gradient in the radial direction is zero
- The cylinder is thermally isolated
- The heat transfer rate from fluid to solid at any point is proportional to the average difference in temperature between fluid and solid at that point

The two coupled PDEs (see [12,15,16,21] for the derivation and further details) take the form

$$\frac{\partial T_f}{\partial t} = -\frac{\dot{m}_f C_{P,f}}{\rho_f \ \varepsilon \ C_{V,f} A} \frac{\partial T_f}{\partial x} + \frac{h_V}{\rho_f \ \varepsilon \ C_{V,f}} \Big(T_b - T_f \Big), \tag{1}$$

$$\frac{\partial T_b}{\partial t} = \frac{6h}{\rho_b d_s C_{V,b}} \Big(T_f - T_b \Big), \tag{2}$$

$$h = \frac{k_f}{d_s} \left(2 + 1.1 \left(\frac{C_{P,f} \mu_f}{k_f} \right)^{1/3} \left(\frac{\dot{m}_f d_s}{A \mu_f} \right)^{0.6} \right),$$
(3)

$$h_V = \frac{6h(1-\varepsilon)}{d_S},\tag{4}$$

where the meaning of the parameters is explained in the following table (the subscript b refers to the solid bed and the subscript f refers to the fluid respectively);

 TABLE I.
 MEANING OF PARAMETERS

Parameter	Unit	Description
\dot{m}_{f}	kg/s	Massic flow of the HTF
$C_{\mathrm{V},f}$ / $C_{\mathrm{V},b}$	J/kgK	Specific heat at constant volume
$C_{\mathrm{P},f}$ / $C_{\mathrm{P},b}$	J/kgK	Specific heat at constant pressure
3	[0,1]	Bed void fraction
ρ_f / ρ_b	kg/m ³	Density
А	m^2	Tank cross section
h	Wm ² /K	Heat transfer coefficient
d_S	m	Average diameter of the packet
		bed particles
k_f	W/mK	Thermal conductivity of the fluid
μ_{f}	Pa s	Dynamic viscosity of the fluid

Defining the next functions

$$C_1(\dot{m}_f, T_f) = \frac{\dot{m}_f C_{P,f}}{\rho_f \epsilon C_{V,f} A}$$
(5)

$$C_2(\dot{m}_f, T_f) = \frac{h_v}{\rho_f \epsilon C_{V,f}}$$
(6)

$$C_3(\dot{m}_f, T_f, T_b) = \frac{6h}{\rho_b * d_S * C_{V,b}}$$
(7)

model (1)-(2) can be rewritten in the more compact form

$$\frac{\partial T_f}{\partial t} = -C_1 \frac{\partial T_f}{\partial x} + C_2 (T_b - T_f), \qquad (8)$$

$$\frac{\partial T_b}{\partial t} = C_3 \Big(T_f - T_b \Big), \tag{9}$$

Air is adopted as the HTF. All thermo-physical properties of the air are dependent on the temperature T_f (see Fig. II). The material chosen for the particles is mostly composed of aluminum oxide, and its thermo-physical properties are also assumed to be dependent on the temperature T_f (see Fig. II). The average diameter of the packet bed particles is $d_s=0.008$ m, whereas the bed void fraction is $\epsilon=0.39$. The temperatures of the hot and cold mass air flow are

The temperatures of the lot and 80 m mass an now are $T_{hot}=237 \text{ °C}$ $T_{cold}=38 \text{ °C}$ (10) that define the admissible operating range for the temperature profiles in the system, whereas a constant airflow is considered in the loading and unloading phases, namely

$$\dot{m}_f = 0.15 \text{ kg/s}$$
 (11)

The coefficients C_1 , C_2 , C_3 depend on the air flow \dot{m}_f of the HTF, and furthermore they also vary with the temperature due to the temperature-dependent thermophysical parameter values. The geometrical properties of the tank are:





FIGURE I. LABORATORY SETUP SCHEMATICS (LEFT) AND PICTURE (RIGHT)

The nonlinear functions C_1 , C_2 , C_3 are averaged by considering (11) and the admissible temperature range (10), yielding the **constant** values

• C1=2,3406 (12)



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• C2=201,1818 (13)

Once the above constant values are replaced into (8)-(9) the original model turns out to be locally linearized and becomes time-invariant. In the next subsection a lumped-parameter finite-dimensional approximation is devised.



FIGURE II. THERMOPHYSICAL PROPERTIES OF AIR AND ALUMINA WITH VARYING TEMPERATURE

A. Finite-dimensional LTI model based on finite-difference method

The spatial domain [0,L] is discretized by a uniformly spaced grid $x_i = i \, dx$, where i=0,1,...,M and dx = L/M. M denotes the number of chosen discretization points.

$$T_{fi}(t) = T_f(x_i, t)$$
 (15)
 $T_{bi}(t) = T_b(x_i, t),$ (16)

Approximating the spatial derivative by finite difference method, the following state equation arise:

$$\frac{\partial T_{fi}}{\partial t} = -C_1 \frac{T_{f_{i+1}} - T_{f_{i-1}}}{2\Delta x} + C_2 (T_{bi} - T_{fi}), \ 1 \le i \le M - 1 \ (17)$$

$$\frac{\partial T_{fM}}{\partial t} = -C_1 \frac{T_{f_M} - T_{f_{M-1}}}{\Delta x} + C_2 \left(T_{bM} - T_{fM} \right) \tag{18}$$

$$\frac{\partial T_{bi}}{\partial t} = C_3 \left(T_{fi} - T_{bi} \right). \quad 1 \le i \le M$$
⁽¹⁹⁾

 $T_{f}(t) = [T_{f1}(t), T_{f2}(t), \dots, T_{f,M-1}(t) T_{f,M}(t)]$ (20)

$$T_{b}(t) = [T_{b1}(t), T_{b2}(t), \dots, T_{b,M-1}(t) T_{b,M}(t)]$$
(21)

The spatial and temporal steps

$\Delta x=0.025$ m Spatial discretization

 $\Delta t=0.0025$ s Temporal discretization

are chosen in order to satisfy (for each admissible temperature and flow values) the inequality

$$CFL = \frac{\dot{m}_f C_{P,f}}{\rho_f \varepsilon C_{V,f} A} \frac{\Delta t}{\Delta x} < 1$$
⁽²⁶⁾

involving the so-called Courant-Friedrichs-Lewy (CFL) number. The chosen spatial discretization yields $L/\Delta x=72$ spatial "nodes", the value M=72 is thus adopted. The state vector is defined as

$$T(t) = \begin{bmatrix} T_{f1} & T_{f2} & \dots & T_{f72} & T_{b1} & T_{b2} & \dots & T_{b72} \end{bmatrix}^{T}$$
(22)

and the corresponding lumped-parameter model is derived as

$$\dot{T}(t) = AT(t) + BT_{f,0}(t)$$
 (23)

with the matrices A and B as follows

$$A = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix}$$
(24)
$$A_{11} = \begin{bmatrix} -C_{2} & -\frac{C_{1}}{2dx} & 0 & \cdots & \cdots & \cdots & 0 \\ \frac{C_{1}}{2dx} & -C_{2} & -\frac{C_{1}}{2dx} & 0 & \cdots & \cdots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \cdots & \ddots & \ddots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \cdots & \cdots & \ddots & \ddots & \ddots & \ddots & 0 \\ \vdots & \cdots & \cdots & \ddots & \frac{C_{1}}{2dx} & -C_{2} & -\frac{C_{1}}{2dx} \\ 0 & \cdots & \cdots & 0 & \frac{C_{1}}{dx} & -\frac{C_{1}}{dx} - C_{2} \end{bmatrix}$$
$$A_{12} = \begin{bmatrix} C_{2} & 0 & \cdots & 0 \\ 0 & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & 0 \\ 0 & \cdots & 0 & C_{2} \end{bmatrix} A_{21} = \begin{bmatrix} C_{3} & 0 & \cdots & 0 \\ 0 & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & 0 \\ 0 & \cdots & 0 & C_{3} \end{bmatrix}$$
$$B = \begin{bmatrix} -\frac{C_{1}}{2dx} \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

and the temperature profile $T_{f,0}(t)$ defining the corresponding Dirichlet boundary condition.

III. OBSERVER DESIGN AND EXPERIMENTAL RESULTS

In the experimental prototype the fluid temperature T_f is measured by temperature sensors embedded into the tank at 19 different vertical locations uniformly spaced along the height



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L of the tank. The available measurements are a subset of the states of the vector T(t), defined by an output matrix C. The first and last sensors measure the temperature at the top (x=0) and bottom (x=L=1.8m) side of the tank. Since the height of the tank is L=1.8m, the spacing between the thermocouples is thus 0.1m.

On the basis of model (23), the Luemberger observer is correspondingly designed as follows

$$\hat{T}(t) = A\hat{T}(t) + BT_{f,0}(t) + K_0 \left(T_{meas}(t) - C\hat{T}(t)\right)$$
(25)

The number m of measurements passed to the observer is changed from m = 7 to m = 1 during several distinct observer design problems under different information availability.

The observer design entails finding an observer gain matrix K_0 such that the eigenvalues of the matrix $A-K_0C$ lie in the open left plane. The spectrum of eigenvalues of matrix A is entirely contained in the left half plane (see Fig. III) and is composed of two separated branches of "fast" eigenvalues (Fig III-top) and "slow" eigenvalues (Fig. III-bottom)



TOP: HIGH FREQUENCY EIGENVALUES. DOWN: LOW FREQUENCY EIGENVALUES

Being the system observability matrix ill-conditioned, the location of the eigenvalues of matrix $A-K_0C$ cannot be set arbitrarily. The matrix K_0 is computed by means of the Matlab

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place() function to move to the left the low frequency branch of eigenvalues (see the bottom Fig. III) by a fixed amount p.

Figure IV shows the results of a first test, where the observer was designed assuming the availability of 7 distinct equispaced measurements. The largest value of p yielding a stable observer dynamics was found as $p=p_{max}=0.01$, and adopted in the test. Figure IV compares the observed and measured temperature profiles in sensor locations that were not used for designing the observer. The dashed lines denote the observed profiles, whereas the continuous lines denotes the measured ones. The vertical dashed line denotes the end of the charging phase (the system is charged when the temperature of the fluid at the lower end of the cylinder is rising by 7.5 degrees from the initial value.)



FIGURE IV OBSERVED AND MEASURED TEMPERATURE PROFILES WITH $m{=}7$ and $p{=}{=}p_{max}$ =0.01

Figure V depicts the corresponding actual and observed **percentage of charge** PoC, computed through the formula



FIGURE V OBSERVED AND ACTUAL PoC WITH m=7 AND DIFFERENT VALUES OF p



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It can be seen from the curves in figure V that the higher p is chosen, the faster the convergence of the estimate, but the higher as well the transient oscillations.

In the last test, only a single measurement was passed to the observer. The maximal admissible value for p in this test was $p=p_{max}=0.0007$. Figure VI compares the performance obtained using different sensor locations (namely, sensor #2, #10 and #18). It emerges that using the sensor located in the upper part of the tank (#2) yields higher transient oscillations of the estimate. Such a transient oscillations is strongly attenuated when the sensors #10 and #18 are used. Besides, comparing Figures V and VI it turns out, as expected, that using an higher number m of measurement sensors in the observer allows a faster reconstruction of the PoC.



FIGURE VI OBSERVED AND MEASURED PoC WITH m=1 AND DIFFERENT SELECTION OF THE MEASUREMENT POINT

IV. CONCLUSIONS

With reference to the packed-bed heat storage apparatus, a Luenberger state observer has been designed, and experimentally verified, in order to reconstruct the internal fluid and packed-bed temperature profiles and the percentage of charge of the tank. Further activities will investigate different observer designs such as Extended Luenberger observer or Kalman filters. Besides, the design of an infinite dimensional observer, not relying on any prior discretization of the mathematical model, is under investigation.

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