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# Mechanical model for 2D steel joints with beams of different depth without web stiffeners.

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*Abstract*— Joints play a very important role in steel structures from the points of view of safety and optimization. In recent years progress has been made in the characterization of the behaviour of steel joints. Part of the knowledge has been integrated in the design codes, and EC3 in particular. In this code the component method has been proposed for connection analysis. However, not all the possible cases are included. One of the configurations that need to be studied is the joint studied in this research: it is a welded internal joint with beams of different depth and without stiffeners. A parametric analysis, based on previously calibrated finite element models is carried out. From the results of this analysis, the expressions for the components that form the mechanical model of the joint are proposed.

*Keywords*— Semirigid joints, Steel structures, Mechanical model, Parametric analysis

# I. Introduction

In the last years an important research has been done with the aim of advancing the knowledge on the behaviour of steel joints under the point of view of stiffness and resistance. In this sense, it is worth mentioning the works of Krawinkler et al. [1], Faella et al. [2], Curtis and Greiner [3], and Hashemi and Jazany [4]. Eurocode 3 [5] uses the component method for the analysis of the 2D joints. This method is difficult in its application, and is not applicable in several of the habitual joints. Recently, Bayo et al. [6] [7] & [8], M. Lopez et al. [9] and A. Loureiro et al. [10] have studied joints with additional plates, the interaction between axes in 3D joints, the behaviour of trapezoidal column web in shear, and that of the double web panel with stiffeners. This research has lead to the development of mechanical models and cruciform elements that take into account the real dimensions of the joints and avoid the use of the  $\beta$ parameter proposed in the EC3.

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E. Bayo University of Navarra Spain One of the joints that have not yet been analyzed in depth, is the joint proposed in the present work. It is a 2D beam to column welded connection, with beams of different depth in both sides of the column, and without stiffeners in the column web. In order to study the joint, calibrated finite elements models have been used. The methodology for determining the stiffness of the different components of the proposed mechanical model is similar to that previously used in other works done by the same authors. This leads to the proposal of a formulation for the different components that constitute the mechanical model of the joint.

## п. Parametric analysis

The parametric analysis has been done using the Abaqus program. The numerical models have been calibrated with the results of previous studies of Loureiro et al [10]. Nonlinear analysis has been used, to take into account the nonlinearity of the material. The real mechanical properties of the material have been introduced in the analysis. The Von Misses yield criterion was selected to define the inelastic response. The finite elements models were performed using Abaqus with solid elements (C3D8R) featuring reduced integration and hourglass control.

In the parametric analysis a total of 16 different configurations have been studied. Table 1 shows those configurations.

TABLE I. CONFIGURATIONS OF THE PARAMETRIC ANALYSIS

Model	Column	Beam 1	Beam 2
M1	HEA200	HEB300	HEB140
M2	HEA200	HEB300	HEB160
M3	HEA200	HEB300	HEB180
M4	HEA200	HEB300	HEB200
M5	HEA200	HEB400	HEB180
M6	HEA200	HEB400	HEB200
M7	HEA200	HEB400	HEB240
M8	HEA200	HEB400	HEB260
M9	HEA240	HEB300	HEB140
M10	HEA240	HEB300	HEB160
M11	HEA240	HEB300	HEB180
M12	HEA240	HEB300	HEB200
M13	HEA240	HEB400	HEB180
M14	HEA240	HEB400	HEB200
M15	HEA240	HEB400	HEB240
M16	HEA240	HEB400	HEB260



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Figure 1. Finite element model



Figure 2. Von Misses stress when loading the deep beam



Figure 3. Von Misses stress when loading the shallow beam

Figure 1 shows a detail of the finite element model. Figures 2 and 3 show the Von Misses stresses when loading the deep beam and the shallow beam, respectively. It can be seen how, when the deep beam is loaded, the stresses extend over the whole panel, and when the shallow beam is loaded, the stresses are confined in a web area corresponding to the height of this beam.



Figure 4. Elastic normal stresses when loading the deep beam



Figure 5. Elastic normal stresses when loading the shallow beam

Figures 4 and 5 show the tension and compression stress contours when loading the deep and the shallow sides, respectively. When the load is applied to the shallow side the compression coming from the lower flange of the shallow beam, is transmitted to the deep beam web. Consequently, it becomes necessary to include this effect in the mechanical model by means of the corresponding spring (component), as it will be explained below.

The moment-rotation curves have been obtained from the finite elements models for both, the deep and shallow beam sides. The study is centered in the linear range, with the aim of determining the stiffness of the joint in both cases. Thus, the results of stiffness for the posterior calibration of the mechanical model are obtained.

# ш. Mechanical Model

The proposed mechanical model is based in previous works developed by Bayo et al [7] [8]. The configuration of the model can be seen in Figure 6.



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Figure 6. Mechanical Model

Most of the springs that configure the mechanical model and simulate the different components of the joint, have been described already in Loureiro et al [10]. Nevertheless, in the present research, in order to obtain the correct calibration of the mechanical model corresponding to the joint under study, the following components are developed:

h: equivalent height of the joint

 $h = h_{db} + t_{fdb}/2$ 

where,  $h_{db}$  is the height of the deep beam and  $t_{fdb}$  is the flange thickness of the deep beam.

 $h_u$ : equivalent height of the upper part of the panel

$$h_u = h_{sb} + t_{fsb}/2$$

where,  $h_{sb}$  is the height of the shallow beam and  $t_{fsb}$  is the flange thickness of the shallow beam

 $h_l$ : equivalent height of the low part of the panel

 $h_l = h - h_u + t_{fdb}/2$ 

where,  $t_{fbb}$  is the flange thickness of the deep beam

 $K_{pl}$ : stiffness of the equivalent spring of the lower column panel:

 $K_{pl} = 1.2 \ G \ A_{vc} \ h_l$ 

 $K_{pu}$ : stiffness of the equivalent spring of the upper column panel:

 $K_{pu} = 1.25 \ G \ A_{vc} \ h_u$ 

where, G is the shear modulus and  $A_{vc}$  is the shear area of the column panel, as defined below (Krawinkler et al [1]):

$$A_{vc} = \left(h_c - t_{cf}\right) t_{cw}$$

where,  $h_c$  is the height of the column,  $t_{cf}$  is the thickness of the column flange and  $t_{cw}$  is the thickness of the column web

 $K_{2m}$  stiffness of the equivalent spring in the web of the deep at the height of the lower flange of the shallow beam:

$$K_{2m} = 0.7 \ h_{db} \ t_{wdb} \ E \ / \ L_{e_f}$$

where, *E* is the Young's modulus,  $t_{wdb}$  is the thickness of the deep beam web and  $L_{ef}$  is the equivalent length of the axially loaded zone of the deep beam web, as shown below:

$$L_{e_f} = 2.5 \ h_{db}$$

 $k_d$  is the stiffness of column web in compression and tension in the deep side.

$$k_d = 0.7 \ h_{e_{ffd}} \ t_{cw} \ E \ / \ d_c$$

where,  $h_{effd}$  and  $d_c$  are the equivalent height and length of the axially loaded zone of the deep beam web, respectively, as defined below:

$$h_{effd} = t_{fdb} + 2\sqrt{2} t_{sol} + 5 (t_{cf} + r_c)$$
$$d_c = h_c - 2 (t_{cf} + r_c)$$

where,  $t_{sol}$  is the throat thickness of the beam flange to column flange weld, and  $r_c$  is the according ratio of the column. (1)

 $k_s$  is the stiffness of column web in compression and tension in the shallow side.

$$k_s = 0.7 h_{e_{ffs}} t_{cw} E / d_c$$

where,  $h_{effs}$  is the equivalent height of the axially loaded zone of the shallow beam web, as shown below:

$$h_{effs} = t_{fsb} + 2\sqrt{2} t_{sol} + 5 (t_{cf} + r_c)$$

The stiffness of the rest of springs become:

$$k_{1T} = 1.2 \cdot k_s \tag{3}$$

$$k_{1M} = 1.2 \cdot k_s$$

$$k_{2T} = 1.8 \cdot k_d$$

$$k_{2B} = 1.8 \cdot k_d$$
IV. **Results** (4)

Once the mechanical model has been developed, the values of stiffness corresponding to the joints that have been analyzed in the FEM parametric study are compared to those obtained with the mechanical models. Figures 7 and 8 show the comparison for the deep and shallow beam, respectively.







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#### Deep side stiffness 80 70 60 (KNm/mrad) 50 40 30 11 30 20 10 0 80 0 10 20 30 40 50 60 70 K<sub>FEM</sub> (KNm/mrad)

Figure 7. Comparison of the stiffness at the deep side between the FEM and the mechanical model when loading the deep beam



Figure 8. Comparison of the stiffness at the shallow side between the FEM and the mechanical model when loading the shallow beam

It can be seen that the results are quite accurate. The normalized mean value for the deep stiffness is 0.993 and the value of standard deviation of 0.027. The mean value for the shallow stiffness is 1.046 and 0.012 for the standard deviation.

# v. Conclusions

In the present research the behaviour of welded 2D beam to column steel joints with beams of different depth without web stiffeners have been carried out. A wide parametric analysis has been done based on previously calibrated finite elements models. The results of these analyses have been used to develop the formulation of the proposed mechanical model. The components of the mechanical model have been obtained.

It must be highlighted the presence of the component corresponding to the deep beam web in compression and tension  $K_{2m}$ .

The results of the proposed mechanical model are very close to those obtained from the refined finite element models.

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