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2-D Online Changepoint Detection Algorithm for Sensor-based Fault Detection

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Abstract—An online 2-D changepoint detection algorithm for sensor-based fault detection, is proposed. The algorithm consists of a differential detector and a standard detector and can detect anomalies and meaningful changepoints while maintaining a low false-alarm rate. The efficiency of the algorithm is validated by two industrial examples. It is thereby shown that the proposed algorithm can be used as an early warning indicator and prevent impending unit failures.

Keywords—Fault Detection, FDI, Changepoint Detection

Introduction

Detecting novelties in the temporal evolution of a system (physical, mechanical, financial, etc.) has received great attention over recent times (see for example [2], [3]). When dealing with complex systems, it is often the case that only a limited understanding of the underlying relationships between various system components can be obtained. Therefore, it immediately follows that a large number of "abnormal modes", some of which may not be known apriori, exist. One approach to address this issue is by using novelty detection schemes (see [1] for a comprehensive survey) where a description of normality is learned by constructing a model with a number of previously seen examples of the normal system behaviour. Previously unseen data is then compared with the derived model, often generating a novelty score. This score is compared against a decision threshold, and the data is then considered to be "abnormal" if the threshold is exceeded.

Changepoint detection [4], [5] is a well-established class of novelty detection schemes where the aim is to detect whether the general distribution of a sequence of observations has remained steady or has undergone some abrupt change. The typical approach to this problem is to find a statistic appropriate for testing the hypothesis that a change has occurred with respect to the hypothesis that no change has occurred.

Given a data sequence that includes abrupt changes, a desirable changepoint detection algorithm must be able to distinguish between "important" and "unimportant" changes. Clearly, what is interpreted as "important" depends on the application and varies by context.

The problem of fault detection and isolation has been studied extensively (see e.g. [20]). In this paper, an online 2-D changepoint detection algorithm for highly correlated data is developed to address the fault detection problem in the relevant fields such as sensor networks.

This paper is organised as follows. A brief overview of change-points and changepoint detection is given in Section II and the choice of online/offline detection is discussed. Welford's method that is used to compute the "online"

standard deviation is described in Section II-A. An online 2-D changepoint detection algorithm is proposed in Section II-B and its efficiency is tested with two industrial examples in Section III.

п. Changepoint Detection

From a statistical perspective, abrupt variations that change the probability distribution of a stochastic process or time series are referred to as changepoints. Often, these variations can be important, indicating an interesting event (e.g., a failure), or unimportant, indicating an expected change. Changepoint detection concerns identifying the times when these important variations occur.

The problem of change-point detection has been actively studied over the last several decades. A typical statistical formulation of change-point detection is to consider probability distributions from which data in the past and present intervals are generated, and regard the target time point as a change- point if two distributions are significantly different. Various approaches to change-point detection have been investigated within this statistical framework, including the CUSUM (cumulative sum) [5] and GLR (generalized likelihood ratio) [6], [7] approaches.

Changepoint detection algorithms are generally classified as "online" and "offline" based on their deployment method. In an online algorithm, a streaming signal is given without any information regarding its future behaviour. The algorithm then aims to detect a changepoint as it occurs while keeping the rate of false alarms to a minimum. Conversely, when using an offline algorithm, the whole signal is given and the goal usually is set to detect all the changepoints in a sequence with an estimation of their occurrence. It should be noted that choice of offline or online depends heavily on the application. However, when dealing with fault detection it is desired to detect a failure as soon as it occurs. Therefore, an online algorithm is presented.

As an online and offline signal processing tool, changepoint detection has been demonstrated to be effective in application areas such as process control [8], EEG analysis [9], [10], [11], DNA segmentation [12], econometrics [13], [15], and disease demographics [14].

In what follows, an efficient and reliable method for computation of the statistics for online changepoint detection is discussed with a focus on fault detection in industrial systems.

A. Welford's Method

The problem of calculating the variance of n data points $\{x_i\}$



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can be difficult, particularly when the number of data points is large and the variance is small. Consider the sequence $X = \{x_1, \dots, x_n\}$, an unbiased estimate of the sample variance σ^2 can be straightforwardly calculated from:

$$S^{2} = \frac{1}{n(n-1)} (n \mathop{\overset{n}{\otimes}}_{i-1}^{n} x_{i}^{2} - (\mathop{\overset{n}{\otimes}}_{i-1}^{n} x_{i})^{2}). \tag{1}$$

From (1), it is readily seen that the computation of variance is carried out in two phases: Firstly to compute the mean over the data and then to calculate sum of the squares of the x_i 's. Variance calculation algorithms play an important role in computational statistics. It is often useful to be able to compute a running variance (i.e., in one pass) for a stream of values, e.g., when costs of memory access dominate those of computation.

Moreover, although (1) appears applicable in simple cases, in scenarios where the standard deviation is relatively small compared to the mean, using (1) can lead to catastrophic

cancellation [16], [17]. That is,
$$n \stackrel{n}{\overset{n}{\circlearrowleft}} x_i^2$$
 and $(\stackrel{n}{\overset{n}{\circlearrowleft}} x_i)^2$ may

be considerably large in practice and calculated with significant rounding error. Therefore, if the variance is small, these numbers cancel out almost completely once subtracted (or even resulting in a negative σ^2 in some cases).

To avoid such issues, a number of alternative algorithms have been proposed (see e.g., [16], [18], [19]) one of which is the iterative algorithm proposed by Welford [16]. This method is based on an iterative formulation:

$$\begin{split} M_{1,j} &= M_{1,j-1} + \frac{1}{j} (x_j - M_{1,j-1}) \\ S_{1,j} &= S_{1,j-1} + (j-1)(x_j - M_{1,j-1}) (\frac{x_j}{M_{1,j-1}}), \end{split}$$

where,

$$T_{i,j} \coloneqq \sum_{k=1}^{j} x_k, \mathsf{M}_{ij} \coloneqq \frac{1}{\mathsf{j}-\mathsf{i}+1} \mathsf{T}_{ij}, \mathsf{S}_{ij} = \sum_{k=1}^{\mathsf{j}} (\mathsf{x}_k - \mathsf{M}_{ij})^2,$$

with $M_{II} = x_I$ and $S_{I,I} = 0$. T_{ij} and M_{ij} are used to denote the sum and the mean of the data points from x_i to x_j respectively.

In this method, each iteration consists of updating M_{ij} by the addition of a single data point and the algorithm requires only one pass of the data. The desired value of S is ultimately obtained as $S_{1,n}$ and therefore, the sample variance is calculated as S/(n-1).

B. Welford's Method

Consider that $N \ge 2$ sequences of highly correlated streaming data are given. In this section, a 2-D changepoint detection algorithm is introduced that detects possible changepoints online, while maintaining a low false-alarm rate. For this

purpose, two detectors are developed; the differential detector that considers changes among the streams, and the standard detector which looks for possible changepoints within the streams individually. The detectors are executed concurrently as the data is streamed and return a flag once a pre-defined threshold is exceeded. If either detector returns a flag, this is recognised as an early warning of a possible development of a changepoint. However, if both detectors return a flag, it is concluded that a changepoint has occurred.

Consider the sequence of received signals x = x[1], x[2], ..., x[N] at time t. The differential detector computes the standard deviation of the *i*-th signal from the mean of $x - \{x[i]\}$, $i \in \{1, 2, ..., N\}$ and compares it against a threshold (see Algorithm 1). Since the data is highly correlated, if x[i] differs significantly enough to pass the threshold (Threshold₁), from the rest of the sequence, it triggers the flag.

Algorithm 1: Differential detector algorithm

For construction of the standard detector, a sequence of sliding windows are used that hold the L recent points, considered here as the *sample*. Lengths of the windows are fixed so when the new signal sequence arrives, the data points at the end of the windows are dropped to maintain the length. Moreover, the whole observed signal received up to the current time step is referred to as the *population* (see Figure 1).

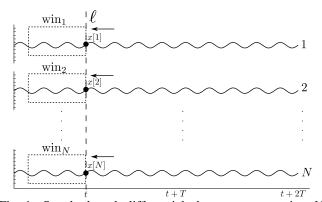


Fig 1. Standard and differential detectors processing N streams of data.

The standard detector is constructed by calculating the distance from the sample mean (M) to the population mean (μ) in units of standard error:

This is commonly referred to as the *standard score*, hence the name of the detector.



Welford's method, described in II-A, is used to calculate the standard score. The score is used to determine the difference between the incoming data stored in the windows and the data previously observed. If this difference exceeds a certain threshold (Threshold₂), a flag is raised. A detailed description of this method is given in Algorithm 2.

```
Initialise: signal size = 0;
          L = size (win);
          S = zeros(N);
          std score = zeros (N);
          mean win = zeros (N);
          mean global = zeros(N);
while Receiving data do
   Let: x = \text{new data};
   Let: mean old = mean global;
   Compute:
                            old+(v-mean old)
                            (signal size+1)
   Let: mean global
   for i = 1 to N do
       w[i].append (x[i]);
       mean_{win}[i] = Mean(w[i]);
                     mean global-mean |i| win
   increment: signal size
```

Algorithm 2: Standard detector algorithm

Notation	Definition
N	number of data lines
x	new data sequence with size n
S	variable for the Welford's method
ω	sequence of N windows
L	size of the window
mean win	mean of the window
mean global	mean of the whole signal received so far
mean old	last computed mean of the whole signal received so far
mean _{new}	new mean of the whole signal received so far
signal size	size of the data received so far
std global	standard deviation of the whole signal received so far
std score	Number of standard deviations an observation is above or
	under the mean
SE	Standard error of the whole signal received so far

TABLE I. NOTATIONS

The whole process of the proposed changepoint detection can be seen in the flowchart depicted in Figure 2.

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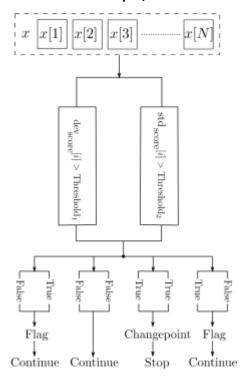


Fig 2. Changepoint detection flowchart

ш. Experimental Case Study

Using the algorithm developed in Section II-B, in this section the problem of fault detection in industrial gas turbine burners is investigated. The gas turbines of interest here normally have 6 burners that are placed in an annular displacement, as seen in Figure 3.

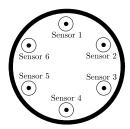


Fig 3. Annular array of burners in the combustion system

Considering the close proximity of the burners, it is expected that the designated sensors roughly read a similar temperature, which results in a highly correlated data set. It is important to note that this data can contain abrupt changes not because of failures, but due to other conditions like noise, changes of load and shutdowns, which are considered "normal".

In this setting, it is crucial to determine whether an observed changepoint is an indication of an actual failure or other possible factors to keep the false-alarm rate to minimum.



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A. Malfunction of One of The Burners

The first scenario is a malfunction on the 6th burner that starts to develop on day 15 of the observation (see Figure 4). As can be seen, after the 15th day, the measurement from Sensor 6 deviates from its previous trend and drops significantly until it reaches a steady state a few days after, while the remaining sensors read the expected temperature. It is worth noting that from the beginning of the observation, Sensor 6 is reading a slightly higher temperature when compared to the others. Moreover, Sensor 4 is reading a lower temperature for the early periods of the observation until it converges with the rest approximately on day 8. Although these abnormalities do not indicate a malfunction, it is important that they receive further attention in case they develop into a failure in the future. Thus, it is desired that a flag be raised when the detector receives the corresponding data sequences.

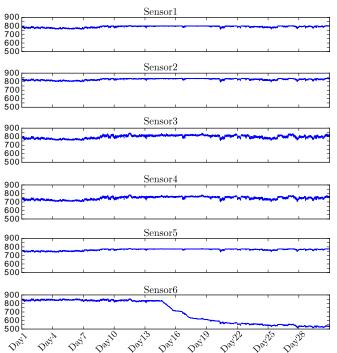


Fig 4. Burner temperatures for 28 days of observation. Sensor 6 indicates a malfunction on day 15.

As can be seen from the results of the proposed changepoint detection algorithm in Figure 5, the anomalies are detected and flagged by the differential detector. The algorithm continues to receive the incoming sequences until both detectors highlight a change on the 15th day. Notably, in this instance, the engine was kept running when this malfunction occurred which could have caused additional ongoing damage.

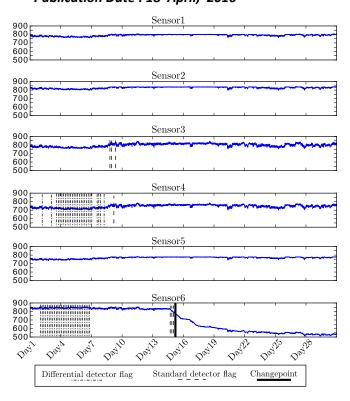


Fig 5. Times when the abnormalities and the changepoint in the data are flagged by either detector.

Calculated deviations and the standard score are plotted in Figures 6 and 7 respectively. From Figure 6, it is readily seen that from the start, sensors 4 and 6 follow a different trend compared to the others. Therefore, the differential detector raises a flag to inform about this abnormality. It is also interesting to note from Figure 7 that one can easily check that the computed standard scores for Sensor 6 deviates from the rest of the sensors almost a week prior to the malfunction.

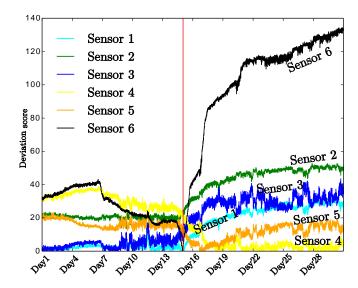
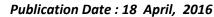


Fig 6. Directional graph of the deviation score computed for each sensor.





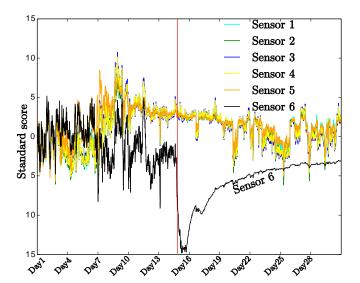


Fig 7. Graph of the standard score computed for each sensor.

B. No Failure on The Burners

In this case, burner temperatures are observed for 1 week. Although no failure occurs, the data contains interesting abnormalities that might be perceived as failures when using alternative algorithms (see Figure 8).

Specifically, on day 2, all temperatures drop abruptly. Although the standard detector captures this sudden change, the differential detector ignores it since all sensors are affected. Thus an alarm is not raised for this incident and the engine can continue to operate. However, it is essential that its performance be monitored carefully since a number of flags are raised.

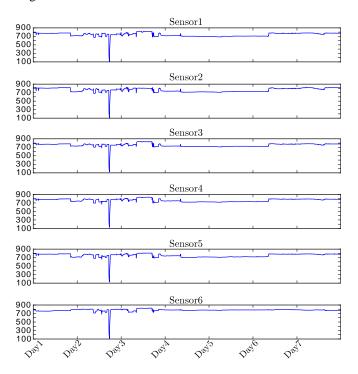


Fig 8. Burner temperatures for 7 days of observation.

Moreover, on the 4th observation day, while the temperature on all sensors marginally drop, Sensor 6 reads a higher

temperature for around 2 days and returns to its normal trend on day 6. Similar to the 2nd day incident, no alarm is raised here since the standard detector's threshold is not exceeded.

Figure 9 shows the times when the abnormalities in the data are flagged by either of the detectors.

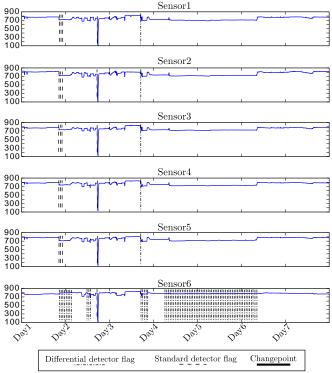


Fig 9. Times when the abnormalities in the data are flagged by either detectors.

Calculated deviations and standard scores are plotted in Figures 10 and 11 respectively. It can be verified from Figure 10 that Sensor 6, shows a different performance compared to the others although the abrupt change of day 2 incurs behaviour similar to the other sensors.

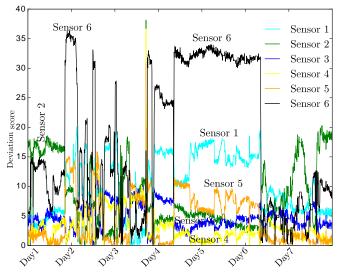


Fig 10. Directional graph of the deviation score computed for each sensor.



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From Figure 11 it can be observed that although the calculated standard score for Sensor 6 is higher than the other sensors on day 2, when the differential detector has raised a flag, an alarm is not triggered since the threshold is not exceeded.

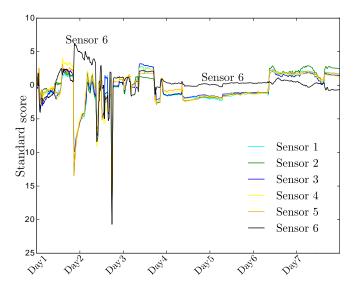


Fig 11. Graph of the standard score computed for each sensor.

In this example, it was seen that although abrupt changes and abnormalities were presented in the temperature measurements, the algorithm correctly did not trigger an alarm.

IV. Conclusion

In this paper, an online 2-D changepoint detection algorithm that detects changepoints in a sequence of correlated streaming data was developed. The detection algorithm uses two detectors namely, the differential detector and the standard detector that look for changepoints among and within the data sequence respectively. The significance of the proposed algorithm is that it reliably detects all of the anomalies that are present in the data and intelligently raises an alarm when an anomaly is deemed to be evidence of an impending failure.

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