

Local Bond Strength based Lap Splice Length Model of Reinforcing Bars

Hyeon-Jong Hwang

Abstract—Lap splice is a critical issue in the structural performance of Reinforced Concrete members. In the present study, the lap splice length of rebars was theoretically studied. On the basis of the bond behavior in the lap splice, a simplified design method was developed to predict the lap splice length of rebars under tension force. In the proposed method, local bond-slip relationship between rebar and concrete was considered. The predicted tensile strength of the splice bars were compared with the 539 existing splice tests results. On the basis of pull-out test results, the proposed model was modified to predict the lap splice length of rebars in the beams using new materials. The predictions agree with the test results.

Keywords—Bond strength, Lap splice length, Splice test, Pull-out test

I. Introduction

Bond strength between rebar and concrete is critical to the structural performance of the Reinforced Concrete (RC) members. For safe design, current design codes [1-3] require the lap splice length on the basis of a lot of splice test results.

To evaluate bond strength of a rebar, four tests are generally performed: pull-out test, beam-end test, beam anchorage test, and splice test (see Fig. 1). Pull-out test is widely used to evaluate the bond strength of a rebar because of the simplicity of the test. However, pull-out test simulates tensile force of a rebar and compressive force of concrete, which differs actual stress field in most RC members where tension force is applied to both the rebar and concrete. Thus, to evaluate the lap splice length, ACI 408-03² recommends not the pull-out test but the splice test.

Orangun et al.⁴ proposed a lap splice length on the basis of a nonlinear regression analysis of existing splice test results. For better predictions, Zuo and Darwin⁵ additionally considered rebar deformed shape and details, and they used not $\sqrt{f'_c}$ but $4\sqrt{f'_c}$ for concrete strength on the basis of existing splice test results. Canbay and Frosch⁶ developed a lap splice model based on the split tension cracking failure, which applied directly the effect cover concrete and lateral bars to bond strength.

Because the previous studies proposed empirical equations to define the lap splice length, the existing models can be used within the verified test parameters. Particularly, assuming the uniformly distributed bond strength in the lap splice length, existing design codes overestimate the bond strength as the lap splice length increases, and the predictions show low correlation with the test results.

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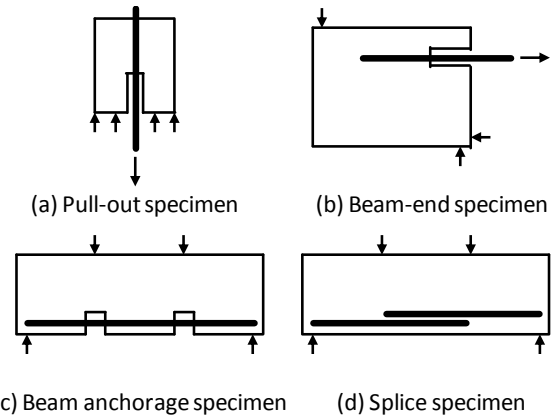


Figure 1. Bond strength test specimens

In order to more accurately predict the lap splice length, in the present study, the following factors are considered. 1) Local bond strength model based on the relative deformation between rebar and concrete was addressed: both the rebar deformation due to bond-slip and tensile deformation of concrete. 2) On the basis of the bond strength distribution in the lap splice length, two idealized bond strength was distributed: non-damaged bond strength and damaged bond strength. To verify the accuracy, the predicted results were compared with the 539 existing splice test results.

II. Proposed Lap Splice Length

A. Simplified Bond Stress Model

Fig. 2 shows the local bond slip-stress relationship between rebar and concrete.^{7,8} In the lap splice length, concrete is vulnerable to cracks of longitudinal direction due to tension force, which decreases the bond strength. Thus, in the present study, local bond stress model for unconfined concrete subjected to tension force was applied. The peak bond stress τ_u and bond-slip s_l are as follows:

$$\tau_u = 0.91\alpha_d \sqrt{f'_c} \quad (1)$$

$$s_l = 0.3\sqrt{f'_c/30} \quad (2)$$

where $\alpha_d = 1.1$ for D19 bars below, 1.0 for D22 to D29 bars, and 0.9 for D32 bars above.

Fig. 3 shows a simplified bond strength model. Although the tension forces are applied to the each rebar at the both sides in the lap splice length, lap splice has the bond mechanism similar to that of anchorage of straight bars. Thus, the present study considered the development length model of a rebar, which used fixed boundary conditions in the concrete at the opposite, to conveniently describe the bond stress distribution and the relative deformation

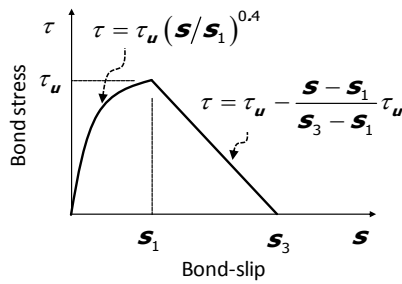


Figure 2. Local bond stress-slip relationship

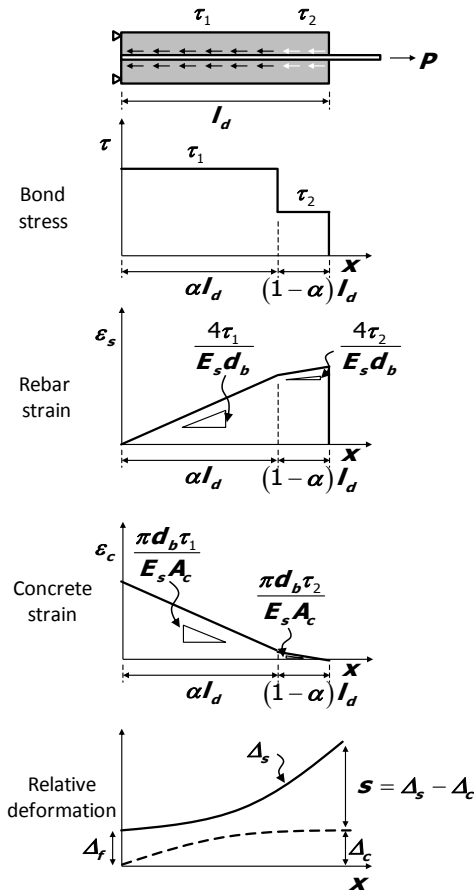


Figure 3. Simplified bond strength model

between rebar and concrete. Note that the lap splice length and development length are not classified (i.e. $l_s = l_d$) in the proposed model. Further, since the relative deformation between rebar and concrete is almost unchanged at αl_d due to tensile deformation of concrete, the bond stress τ_1 and τ_2 are applied to αl_d and $(1-\alpha)l_d$ as uniformly distributed stress, respectively.

On the basis of the simplified bond stress distribution, strain distributions of rebar and concrete can be estimated (refer to Fig. 3). Note that, in structural design, because large inelastic deformation does not occur in the spliced bars, post-yielding behavior of the rebar was not considered.

$$\left(\frac{\pi d_b^2}{4}\right) \frac{d\sigma_s}{dx} = \tau(x)(\pi d_b) \quad (3)$$

$$\epsilon_s - \epsilon_c = ds/dx \quad (4)$$

where d_b = rebar diameter; σ_s = tensile strength of the rebar;

and s = relative deformation of rebar and concrete due to bond-slip.

Absolute deformation Δ_s of the rebar at the peak strength (i.e. at $x = l_d$) can be determined from strain distribution of the rebar.

$$\Delta_s = \int_0^{\alpha l_d} \frac{4\tau_1}{E_s d_b} x dx + \int_{\alpha l_d}^{l_d} \left[\frac{4\tau_1}{E_s d_b} \alpha l_d + \frac{4\tau_2}{E_s d_b} (x - \alpha l_d) \right] dx + \Delta_f \quad (5)$$

$$= \frac{l_d^2}{E_s d_b} \left[(4\alpha - 2\alpha^2)\tau_1 + (2 - 4\alpha + 2\alpha^2)\tau_2 \right] + \Delta_f$$

where Δ_f = absolute deformation of the rebar at zero strain (i.e. at $x = 0$) regardless of strain distribution of the rebar due to pull-out failure. Thus, in the case of pull-out failure of the rebar, Δ_f increases to maximize the bond strength in the development length l_d . When the pull-out failure of the rebar does not occur, Δ_f equals to zero. In the present study, τ_1 is simplified as τ_u assuming the maximum bond strength in the pull-out failure.

Relative deformation s between rebar and concrete is defined by (4).

$$s = \Delta_s - \Delta_c \quad (6)$$

According to the bond stress distribution in Fig. 3, the relative deformation s should be less than or equal to s_1 in the development length αl_d , and s should be greater than s_1 in the development length $(1-\alpha)l_d$ (refer to Fig. 2). Considering that s equals to s_1 at $x = \alpha l_d$ in (5) and (6), s_{ald} is as follows:

$$s_{ald} = \frac{l_d^2}{E_s d_b} \left[2\alpha^2 \tau_1 \right] + \Delta_f - \Delta_c \approx s_1 \quad (7)$$

Substituting (7) to (5) and (6),

$$s = \frac{l_d^2}{E_s d_b} \left[(4\alpha - 4\alpha^2)\tau_1 + (2 - 4\alpha + 2\alpha^2)\tau_2 \right] + s_1 \quad (8)$$

For conservative estimation, when the relative deformation is greater than s_1 , the decreased bond stress τ_2 is defined as the bond stress at the maximum relative deformation. Thus, the decreased bond stress τ_2 can be defined as the function of the relative deformation s in Fig. 2.

$$\tau_2 = \tau_1 - \frac{\tau_1}{1 - s_1} (s - s_1) = \frac{\tau_1 - C_1 \tau_1^2 (4\alpha - 4\alpha^2)}{1 + C_1 \tau_1 (2 - 4\alpha + 2\alpha^2)} \quad (9)$$

where $C_1 = l_d^2 / [(1 - s_1) E_s d_b]$.

In the development length l_d of a rebar, the maximum tensile stress f_s of the rebar is defined as follows:

$$f_s = \frac{4l_d}{d_b} \left[\alpha \tau_1 + (1 - \alpha) \tau_2 \right] \quad (10)$$

where $\alpha=0.75$ predicts well the test results (see chapter "COMPARISON BETWEEN TEST RESULTS AND PREDICTIONS").

B. Effect of Cover Concrete and Lateral Bars

The lap splice length is affected by the effects of split tensile cracks according to cover concrete thickness and spacing of the spliced bars (refer to Fig. 4). Existing design codes considered these effects using same parameters, but the different coefficients were used. In the present study, the method proposed by ACI 408R-03² was used.

For ACI 408R-03

$$\tau_1 = 0.91\alpha_d \sqrt{f'_c} \left[\frac{(cw + K_{tr})/d_b}{2.5} \right] \quad (11a)$$

$$(cw + K_{tr})/d_b \leq 4.0 \quad (11b)$$

$$w = 0.1(c_{\max}/c_{\min}) + 0.9 \leq 1.25 \quad (11c)$$

$$K_{tr} = 6\sqrt{f'_c} t_d A_{tr} / (s_t n) \quad (11d)$$

$$t_d = 0.03d_b + 0.22 \quad (11e)$$

where $c = c_{\min} + d_b/2$; $c_{\max} = \max(c_b, c_s)$; $c_{\min} = \min(c_b, c_s)$; $c_s = \min(c_{so}, c_{si} + 6.4)$; $c_b =$ thickness of the bottom cover concrete; $c_{so} =$ thickness of the side cover concrete; $c_{si} =$ one-half of the center-to-center bar spacing; $A_{tr} =$ total cross-sectional area of transverse bars within spacing s_t that cross the potential plane of splitting; $n =$ the number of bars being developed or spliced along the splitting plane; and $s_t =$ center-to-center distance of the transverse bars. Note that the coefficient of the cover concrete and lateral bars by ACI 408R-03² is divided into 2.5, which is same to the bond strength by ACI 318-11¹ before pull-out failure.

III. Comparison Between Test Results and Predictions

Table 1 presents the test parameters of existing splice specimens. For total 539 specimens, the splice length l_s was 76 to 2311 mm [3.0 to 91.0 in], the rebar diameter $d_b = 9.5$ to 43.0 mm [0.4 to 1.7 in], the concrete strength f'_c was 12.6 to 113.0 MPa [1.8 to 16.4 ksi], and yield strength of the rebar f_y was 345 to 830 Mpa [50.0 to 120.3 ksi].⁹⁻²⁵ Table 2 compares the predictions by the existing design models and proposed model to the test results.

Fig. 5 compares the tensile strength of the rebar predicted by the existing design codes and proposed model to the test results according to the ratio of the splice length to rebar diameter. ACI 318-11¹ underestimated the tensile strength of the rebars f_s , which causes the conservatively designed lap splice length l_s . Particularly, the existing design codes overestimated the tensile strength of the rebars f_s as the lap splice length ratio l_s/d_b increases. On the other hand, ACI 408R-03² (average= 1.00, and COV.= 0.151) and the proposed model using the coefficient of ACI 408R-03² (average= 1.00, and COV.= 0.153) predicted $f_{test}/f_s = 1.0$ in most of specimens.

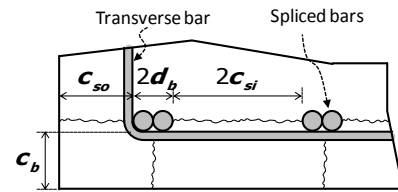


Figure 4. Cross-section of splice specimen

TABLE I. TEST PARAMETERS OF EXISTING SPLICE TEST SPECIMENS

Specimens	# of tests	l_s/d_b	f'_c (MPa)	f_y (MPa)	$(cw+K_{tr})/d_b$
Chinn et al. ⁹	40	9.3-31.9	21.8-51.6	393-545	1.51-3.09
Chamberlin ¹⁰	18	6.0-24.0	30.2-32.0	345	2.63-2.88
Ferguson and Thompson ¹¹	42	18.0-48.0	16.4-41.1	566-604	1.74-4.00
Ferguson and Breen ¹²	35	18.0-80.0	12.6-38.8	428-676	1.89-2.78
Ferguson and Bricker ¹³	32	23.4-60.3	16.9-30.0	449-483	1.25-2.13
Thompson et al. ¹⁴	25	14.2-36.0	17.4-32.5	384-464	1.33-3.16
Zekany et al. ¹⁵	24	14.2-15.6	25.5-39.3	415-433	1.92-2.43
Choi et al. ¹⁶	10	16.0-19.2	37.0-41.5	435-489	1.92-2.31
Azizinamini et al. ¹⁷	18	9.2-56.8	35.1-104.3	489-537	1.48-1.50
Hester et al. ¹⁸	32	10.0-22.8	34.7-44.5	440-499	2.36-4.00
Rezansoff et al. ¹⁹	15	11.9-37.6	25.0-28.2	445-475	1.78-3.52
Azizinamini et al. ²⁰	12	28.4-56.8	75.2-113.9	489-509	1.48-2.34
Darwin et al. ²¹	25	16.0-28.4	26.3-36.2	445-538	2.17-3.74
Azizinamini et al. ²²	70	9.2-56.8	35.1-113.9	489-537	1.50-4.00
Zuo and Darwin ²³	65	16.0-40.0	29.3-108.0	435-556	1.38-3.53
Seliem et al. ²⁴	64	24.0-70.3	28.0-70.3	830	1.68-4.00
Choi et al. ²⁵	12	29.4-60.1	24.7-55.3	650-720	1.80-3.65
Total	539	6.0-80.0	12.6-113.9	345-830	1.25-4.00

TABLE II. COMPARISON BETWEEN TEST RESULTS AND PREDICTIONS

Specimens	f_{test}/f_s (ACI 318-11)	f_{test}/f_s (ACI 408R-03)	f_{test}/f_s (Eurocode 2)	f_{test}/f_s (Prediction)
Chinn et al. ⁹	0.83-2.65	0.69-1.31	0.83-1.91	0.68-1.54
Chamberlin ¹⁰	0.96-2.72	0.62-1.05	0.96-2.77	0.81-1.57
Ferguson and Thompson ¹¹	1.27-2.87	0.65-1.44	1.00-2.15	0.59-1.34
Ferguson and Breen ¹²	0.99-2.43	0.79-1.33	0.90-1.70	0.74-1.33
Ferguson and Bricker ¹³	0.61-2.01	0.58-1.13	0.55-1.28	0.55-1.22
Thompson et al. ¹⁴	1.36-2.37	0.82-1.19	0.94-1.86	0.87-1.36
Zekany et al. ¹⁵	1.41-2.03	0.81-1.24	1.12-1.60	0.82-1.26
Choi et al. ¹⁶	1.21-1.77	0.73-1.24	0.83-1.50	0.79-1.07
Azizinamini et al. ¹⁷	0.90-1.72	0.75-1.04	0.66-0.96	0.66-1.09
Hester et al. ¹⁸	1.15-2.35	0.73-1.32	0.90-1.85	0.58-1.27
Rezansoff et al. ¹⁹	1.59-2.18	0.86-1.22	1.08-1.60	0.92-1.10
Azizinamini et al. ²⁰	0.93-1.14	0.77-1.13	0.66-1.13	0.66-1.13
Darwin et al. ²¹	1.18-2.09	0.83-1.16	1.01-1.68	0.72-1.03
Azizinamini et al. ²²	0.90-1.72	0.74-1.12	0.66-1.12	0.66-1.12
Zuo and Darwin ²³	1.09-2.57	0.87-1.41	0.65-1.73	0.71-1.16
Seliem et al. ²⁴	0.76-2.26	0.76-1.49	0.56-1.52	0.59-1.29
Choi et al. ²⁵	0.95-1.67	0.81-1.15	0.77-1.45	0.77-1.00
Total	0.61-2.87	0.58-1.49	0.55-2.77	0.55-1.57
Average	1.50	1.00	1.14	1.00
COV.	0.267	0.151	0.257	0.153

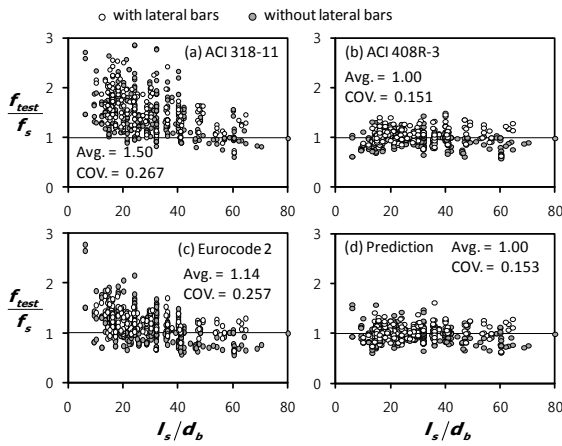


Figure 5. Reinforcing bar stress ratio of specimens according to lap splice length ratio

Note that ACI 408R-03² and the proposed model did not use a safety factor. On the basis of the comparison between predictions and test results, tensile force f_s of rebar and splice length l_s in the proposed model using $\alpha = 0.75$ can be simplified as follows.

$$f_s = \frac{l_d}{d_b} [3\tau_1 + \tau_2] \quad (12)$$

$$l_d = \frac{f_y d_b}{3\tau_1 + \tau_2} \quad (13)$$

$$\tau_1 = 0.91\alpha_d \sqrt{f'_c} \left[\frac{(cw + K_{atr})/d_b}{2.5} \right] \quad (14)$$

$$\tau_2 = \frac{8\tau_1 - 6C_1\tau_1^2}{8 + C_1\tau_1} \quad (15)$$

where $C_1 = l_d^2 / \left[(1 - 0.3\sqrt{f'_c/30}) E_s d_b \right]$.

IV. CONCLUSIONS

In the present study, a simplified model was developed to predict the lap splice length using the local bond strength model according to the relative deformation between rebar and concrete. On the basis of the relative deformation and local bond strength model, bond strength distribution was simplified to two equivalent bond strength: non-damaged bond strength, and damaged bond strength. For the effects of cover concrete and lateral bars, the ACI 408R-03 model was used. The validity of the proposed method was verified using the 539 existing lap splice test results. Existing design codes overestimated bond strength as the lap splice length increases. On the other hand, the proposed method predicted the tensile strength of the spliced bars with reasonable precision.

A. Authors and Affiliations

1) Hyeon-Jong Hwang is an Assistant Professor in the College of Civil Engineering at Hunan University, China. He received his BE, MS, and PhD in architectural engineering from Seoul National University. His research interests include inelastic analysis and the seismic design of RC and composite structures.

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[Lap splice is a critical issue in RC members. In order to more accurately predict the lap splice length, not empirical equation but mechanics based simplified lap splice model is needed.]