# A Method for 3D Reconstruction of ISAR Images Using Impulse-Radio UWB 

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#### Abstract

Recently, the use of Ultra Wide Band (UWB) technology has been increasing. This technology makes it possible to obtain high-resolution images of distant objects using microwave signals. A 2D ISAR algorithm was developed for defense and tomography and is used in medical approach. In this paper, the tomography algorithm is studied, using microwave similar to those used in reflection tomography. Threedimensional images were reconstructed using two receiver antennae and one transmitter. The ISAR interferometry configuration was designed as a backprojection algorithm. When compared to 2D imaging, the signal has an elliptical range profile in the 3D observation mode. An elliptical range migration is confirmed in both theoretical and experimental results.


Keywords- impulse radio UWB, ISAR image, 3D reconstruction, backprojection

## I. Introduction

In the past decade, UWB technology has been developed [1-11] with a bandwidth from 500 MHz up [2-3]. This characteristic makes it possible to obtain high-resolution images of distant objects using microwave signals [4-7]. One of UWB technology can generate an impulse-radio pulse [1, 47], in a short time. These features allow for the reconstruction of quality images, and when using a short pulse, coupling interference and the multipath effect are absent.

Inverse Synthetic Aperture Radar (ISAR) is a powerful tool for imaging moving targets. ISAR 2D images are constructed from the scattered field of a target using its various sights and delay history [13]. Creating different views is simple when using a turntable that can be rotated to the required angle [6-8]. In this fixed geometry, back-projection tomography can be used for image reconstruction. Various studies have been conducted on reconstructing 2D images by using microwave signals [9-12], because these images are projected on rotating plane. Three-dimensional images not only require a projected image but also height information. The current methods of reconstructing 3D images require Cscans to be performed [11], which are physically bulky and time-consuming.

[^0][^1]In general, the reconstruction of 3D images uses a separate receiver for different angles of the rotating plane. A baseline distance between each receiver can be obtained by adding a dimension [9-10]. If the receiver and the transmitter antennae are projected on a $2 \mathrm{D}, \mathrm{X}-\mathrm{Y}$ plane, then 3 D information is estimated from data that is obtained by a separate receiver with a Z axis. The conceptual method of operation to calculate the height of objects is similar to the geometric configuration of delay in the Doppler radar, which is an interferometry altimeter radar able to detect landscape elevation from angle estimation [12].

The objective of this study is to reconstruct 3D images from additional receivers along the Z -axis and to develop a reconstruction signal processing algorithm.

In section 2, a wave model, geometric configuration of equipment and backprojection algorithm, which is a tomography method of obtaining 2D images, are presented. In section 3, the estimation of height is introduced. In section 4, experiment results are discussed, followed by concluding remarks in section 5.

## i. Geometry

## A. Wave Propagation

If the distance between the antennae and the object is far enough, it can be assumed that received and transmitted signals are parallel beam waves. A short pulse model that transmits signals looks like the delta function in (1).

$$
\begin{equation*}
s(t)=\delta(t-\tau) \tag{1}
\end{equation*}
$$

The relation between round trip flight time and range is defined in (2).

$$
\begin{equation*}
r=c \tau / 2 \tag{2}
\end{equation*}
$$

## B. Geometric Configuration

In 2D ISAR, the transmission antenna is assumed to be placed close to the receiving antenna, and the object to be far more than Fresnel region from the antennae on the turn table.


Figure 1. Transmitted signals and antenna configuration
The range, which is the distance between the antenna and object, can be calculated using the law of cosine as shown in (3)

$$
\begin{equation*}
r(\theta)=\sqrt{D^{2}+R^{2}-R D \cos \left(\theta_{0}+\theta\right)} \tag{3}
\end{equation*}
$$

where $r$ is the distance between the antenna and the object, R is the distance between the center of rotation and the object, D is the distance between the center of rotation and the antenna, $\theta_{0}$ is the initial angle of the object, and $\theta$ is the angle of rotation.

When using a parallel or plane wave, the range can be derived as in (4), which shows that received signals can be modeled by a set of lines like those in Figure 1. The geometric model is shown as Figure 2.

$$
\begin{align*}
& r(\theta)=D+R \cos \left(\theta_{0}+\theta\right) \\
& =D+R \cos \theta_{0} \cos \theta-R \sin \theta_{0} \sin \theta  \tag{4}\\
& =D+x \cos \theta-y \sin \theta
\end{align*}
$$

To prove theoretical range migration by slant viewing angle, the ISAR radar system with short pulse UWB radar was used. Figure 3 shows the system configuration. The target on the turn table is rotated with a motion controller.


Figure 2. Geometric model of turning motion


Figure 3. ISAR system configuration

## c. Backprojection

The backprojection algorithm is used to make 2D images from received data [13], [14]. As shown in Figure 1, received signals are given by the sum of scattering on the lines. Equation (5) gives the projection of scattering along an arbitrary line of the $\mathrm{X}-\mathrm{Y}$ plane, and $\mathrm{f}(\mathrm{x}, \mathrm{y})$ refers to the image or real target.

$$
\begin{equation*}
g(\rho, \theta)=\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) \delta(x \cos \theta+y \sin \theta-\rho) d x d y \tag{5}
\end{equation*}
$$

Before reconstructing an image, a 2D inverse Fourier transform of $\mathrm{F}(\mathrm{u}, \mathrm{v})$ is given by (6).

$$
\begin{equation*}
f(x, y)=\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} F(u, v) e^{j 2 \pi(u x+v y)} d u d v \tag{6}
\end{equation*}
$$

The 1D Fourier transform of the received signal is $s(t)$, with respect to time, and the angle is defined in (7).

$$
\begin{equation*}
S_{\theta}(w)=\int_{-\infty}^{\infty} s(t) e^{-j 2 \pi w t} d t \tag{7}
\end{equation*}
$$

According to the Fourier slice theorem, $F(u, v)$ has a symmetric property, and $\mathrm{f}(\mathrm{x}, \mathrm{y})$ can be expressed by the 2 D inverse Fourier transform with polar coordinates, as below (8).

$$
\begin{equation*}
f(x, y)=\int_{0}^{\pi}\left[\int_{-\infty}^{\infty} F(w, \theta)|w| e^{j 2 \pi w t} d w\right] d \theta \tag{8}
\end{equation*}
$$

In practice, the Hamming or Hanning window can be used instead of the ramp filter $|\mathrm{w}|$. This substitution was defined
previously in (8), and the 1D Fourier transform of the received signal is shown in (9) using an independent angle and time.

$$
\begin{equation*}
f(x, y)=\int_{0}^{\pi}\left[\int_{-\infty}^{\infty} S_{\theta}(w)|w| e^{j 2 \pi w t} d w\right] d \theta \tag{9}
\end{equation*}
$$

The filtered signal of this angle is $Q_{\theta}$ and is expressed by the following (10).

$$
\begin{equation*}
Q_{\theta}(t)=\int_{-\infty}^{\infty} S_{\theta}(w)|w| e^{j 2 \pi w t} d w \tag{10}
\end{equation*}
$$

The image can be calculated by (11)

$$
\begin{equation*}
f(x, y)=\int_{0}^{\pi} Q_{\theta}(x \cos \theta+y \sin \theta) d \theta \tag{11}
\end{equation*}
$$

where the equation (11) means that integrals along the lines of each angle of the filtering signal can become a reconstructed 2D image.

## III. Estimation of Height

To acquire height information, both the general 2D ISAR and a different view of the 2D ISAR need to be observed. If we look at the circle of the trajectory of a point target from a higher or lower angle, the circle appears as an ellipse as shown in Figure 2. As the shadow of the circular ring looks like an ellipse, the inclined radar observes projected data on another plane, which means that the direction of the view is dependent on range.

The ellipse center is placed as the origin of the coordinate, and the Cartesian coordinate position is written by (12) and (13) where $a$ is a semi-major axis and $b$ is a semi-minor axis.

$$
\begin{align*}
& y=a \sin \theta  \tag{12}\\
& x=b \cos \theta \tag{13}
\end{align*}
$$

The transmitted signal is assumed to be a plane wave as in the following (14).

$$
\begin{aligned}
& r(\theta)=D^{\prime}(z)+b \cos \left(\theta_{0}^{\prime}+\theta\right) \\
& =D^{\prime}(z)+b \cos \theta_{0}^{\prime} \cos \theta-b \sin \theta_{0}^{\prime} \sin \theta \\
& =D^{\prime}(z)+x^{\prime} \cos \theta^{\prime}-\frac{b}{a} y^{\prime} \sin \theta^{\prime}
\end{aligned}
$$

The above equation (14) is slightly different compared with (4), where the height can be distinguished from the range equation. The modified range equation can be written by (15).

$$
\begin{equation*}
r(\theta)=D^{\prime}(z)+x^{\prime} \cos \theta^{\prime}-\Delta Z y^{\prime} \sin \theta^{\prime} \tag{15}
\end{equation*}
$$

The height can be calculated by eccentricity, b/a, and the distance between the center of the ellipse and the antenna. Height is proportional to $y \sin \theta$. Before estimating height, eccentricity or the viewing angle must be known.

## iv. Results

The radar system is summarized in TABLE 1. Theoretical resolution of the used short pulse corresponds to 1 mm . A short pulse generator requires a high-speed sampling convertor, and the equipment used in this study satisfies this criterion. The chosen angle step is 1 degree and every angle was observed.


Figure 4. Geometrical model of the inclined view of a circular motion.

The observational results from the side view and slant view are shown in Figures 5 and 6. The object used was a 2.5 cm long needle. In Figure 6, the range profile has different flattening and range movement decreased, when compared to Figure 5. Figure 6 also has eccentricity.

TABLE I. RADAR PARAMETERS

| PRF | 1 MHz |
| :---: | :---: |
| Pulse Width | $\sim 30$ pico seconds |
| Number of <br> Average Pulses | 128 |
| Sampling <br> Interval | $3 / 1024$ nano <br> seconds |
| Number of <br> Samples | 1024 |
| Rotation Angle <br> Step | 1 degree |
| Rotation | $1 \sim 360$ degrees |



Figure 5. Side view of sinogram.


Figure 6. Inclined view of sinogram.

## v. Conclusions

The 2D ISAR imaging algorithm for tomography was introduced in this research, which concentrated on reconstructing 3 D images using two different viewing receivers. ISAR interferometry configuration is designed for reconstructing 3D image. In the 3D observation mode, the signal has an elliptical range profile. The short pulse UWB radar was used to ensure that the experiments performed without anechoic chamber conformed to those done anywhere. The results of this research suggest a new methodology for the configuration of observation. In future studies, resolution and analysis should be improved, and a focused algorithm and polar format interpolation of tomography developed.

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